# A Semi-Automatic Procedure for DEM Generation from Stereo Digital Imagery 

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#### Abstract

Digital Elevation Models (DEMs) are currently produced by both manual and automated methods. Manual methods are typically reliable, but are slow and expensive for large areas. Automated methods, which determine the ground surface elevation by matching conjugate image portions, can be fast and relatively inexpensive but fail on complicated scenes and in featureless areas. Such automated techniques require the availability of powerful digital photogrammetric workstation with sophisticated software.

In this research, a semi-automatic procedure is presented to generate DEMs from stereo digital imagery. Here, the operator points to posts of interest in one image and their conjugate points are found, to sub-pixel accuracy, by use of matching. This would assure selecting appropriate matching entities, leading to a minimal number of matching ambiguities. Moreover, this procedure can be implemented on a PC which is always available in places that can not afford costly photogrammetric workstations. The test imagery consists of a stereo-pair of aerial images covering an urban area. The images are scanned with two different resolutions: 200 dpi and 600 dpi. A total of 90 feature points in the overlapping area are selected and matched using correlation technique. ¢The 3-D ground coordinates of the selected points are computed using bundle adjustment with fixed and inner constraints. Prototype software is developed for matching and adjustment computations. The achieved results have shown simplicity and efficiency of the adopted procedure in reconstructing DEMs from digital aerial imagery.


Keywords: Digital Elevation Model, Automated Photogrammetry, Image Matching, Correlation Techniques, Digital Images.

## 1. Introduction

The prevalence of computers has made a significant shift in the way survey and map data are collected, processed, presented and stored. During 1970s, photogrammetric compilers manually traced contour lines from stereo imagery. This contour representation of the terrain, plotted on a stable base material, was the archival medium from which subsequent terrain analysis and engineering design were done. Computer capabilities have introduced two fundamental changes to this process. First, terrain data now are collected mostly as a sequence of discrete data (3-D coordinated points). The terrain data, together with other supplementary data, such as abrupt changes in terrain slope or breaklines, set up a discrete sampling of the continuous terrain surface that should be adequate for its mathematical reconstruction. Second, the archival record has become the digital coordinate file itself rather than a particular graphical depiction, such as contours, profiles, or wire frame perspective views. These depictions can be generated whenever needed as long as the archival data of the original terrain points are available.

DTMs are generally planned such that the collected points lie in a regular grid pattern or represent vertices of local triangular patches in an array referred to as a triangulated irregular network. The advantages of a regular grid layout are a simplified data collection routine, and ease of data access by subsequent programs [5]. The disadvantages are related mostly to the necessity to select a single grid interval, adequate to define the terrain in the roughness area although likely to be over-sampled in regions where the terrain is featureless. Conversely, in the irregular point approach, the sampling interval can change to match the local terrain character. This would optimize the quantity of data necessary to define the terrain. Data access for subsequent software analysis is considerably more involved than when using the simple grid structure.

During the design of a DEM, a quantitative analysis is done to determine the magnitude of the errors expected during reconstruction of the terrain surface. The magnitude of these errors should be within the error budget of potential user or client applications. Given a DEM and interpolation function, one should be able to construct a profile or cross section along any arbitrary path within the area covered. This capability would permit one to interpolate heights at regular grid points from an irregular grid as and to interpolate irregular points from a regular grid. With some cost to accuracy, one could convert between these two popular storage models [6].

Topographic surveys necessary for DEM generation can be performed by photogrammetric methods, terrestrial methods, or some combination of these two procedures. The largest portion of small- and intermediate-scale as well as some large-scale topographic mapping is currently performed by photogrammetric methods. Terrestrial methods are still applicable for large-scale topographic mapping of small areas and for field completion surveys. However, Global Positioning System (GPS) provides a powerful tool for topographic mapping of extended clear-sky regions.

## 2. Photogrammetric Production of DEMs

DEMs are currently produced by both manual and automated methods. In manual production, either the stereoplotters sets the floating mark at the horizontal position of each point and the operator places it on the ground, or the system drives along a profile while the operator keeps the mark on the ground. Automated systems use computer vision techniques to perform the operator's task of determining the ground surface elevation by matching corresponding portions of two stereo images [3,5]. Both production methods have their strengths and weaknesses. Manual methods are typically reliable, but are slow and expensive for large areas. Automated methods can be fast and relatively inexpensive, but fail on complicated scenes, such as urban areas or forests, and in featureless areas.

Manual editing of automated results is nearly always required. Some systems let the operator specify complicated areas so that the stereo matcher skips these areas, leaving them for the operator.

The points obtained by image matching are not evenly distributed and do not completely represent the surface. Even if all pixels were selected in image matching, there will be holes since matching is not always successful [7]. Thus the resulted 3-D points must be interpolated. The term surface fitting is more general as it includes interpolation and approximation methods. Surface fitting methods can be classified according to the criteria such as goodness of fit, extent of support (local versus global) or type of mathematical model (weighted average, polynomials, splines).

In most DEM generating systems, matching and surface densification are truly automatic tasks requiring human intervention only in the beginning to initialize the process. Despite all checks performed by the two tasks, it is essential that the DEM is now checked by a human operator for accuracy and completeness, a process that may be referred to as quality control. This interactive process comprises displaying the DEM and editing the data if necessary. The task is very crucial due to its influence on the quality of the DEM and the economy of automated techniques.

## 3. Digital Image Matching

Image matching, or finding conjugate points automatically, is a fundamental task in photogrammetry. Matching is required in automatic image orientation, automatic aerial triangulation, automatic generation of DEM's and orthoimagery, and object recognition [2,8,10]. The names of matching methods are usually related to the matching primitive, for instance, areabased matching, feature-based matching and symbolic matching.

In area-based matching, gray levels are matched. Here, grey level distribution of small areas of the two overlapping images, named image patches, is compared with each other. The degree of similarity is determined using a maximization criterion such as the cross-correlation coefficient or a minimization criterion as the least-squares technique. In feature-based matching, edges or other features derived from the images are utilized as the matching primitives. Symbolic matching refers to methods that compare symbolic descriptions of images. Symbolic descriptions can be implemented as graphs, trees or semantic nets relating derived image features.

Correlation matching has a well-known procedure for image matching in the field of photogrammetry. The idea is to measure the similarity of the reference window, the image patch that remains fixed in one image, with each of the matching windows in the search window in the other image using the cross-correlation coefficient as follows [6,7]:

$$
\begin{equation*}
\rho=\sum\left(\mathrm{R}_{\mathrm{ij}}-\mu_{\mathrm{R}}\right)\left(\mathrm{S}_{\mathrm{ij}}-\mu_{\mathrm{s}}\right) /\left[\sum\left(\mathrm{R}_{\mathrm{ij}}-\mu_{\mathrm{R}}\right)^{2}\right]^{1 / 2}\left[\sum\left(\mathrm{~S}_{\mathrm{ij}}-\mu_{\mathrm{S}}\right)^{2}\right]^{1 / 2} \tag{1}
\end{equation*}
$$

Where
$\mathrm{R}_{\mathrm{ij}}$ sequence of gray levels contained in the reference window;
$\mathrm{S}_{\mathrm{ij}}$ sequence of gray levels contained in the matching window;
$\mu_{R}$ mean of the sequence of gray levels contained in the reference window;
$\mu_{\mathrm{S}}$ mean of the sequence of gray levels contained in the matching window; and
$\sum \quad \sum_{\mathrm{i}} \sum_{\mathrm{j}}$ with i and j proceeding over the R-S overlap area.

At performing the matching procedure, the cross correlation coefficient is computed for every position of the matching window within the search window. Next, the position that yields the maximum correlation coefficient is to be determined. If the search window is constrained to the epipolar line, the correlation coefficient can be plotted in a graph and the maximum is found by
fitting a polynomial through the correlation values. Otherwise, a two-dimensional polynomial (Eqn. 2 ) is fitted and searched for the maximum.

$$
\begin{equation*}
f(x, y)=a_{0}+a_{1} x+a_{2} y+a_{3} x y+a_{4} x^{2}+a_{5} y^{2} \tag{2}
\end{equation*}
$$

Apart from the used similarity measure, some aspects are crucial and they are to be resolved in order to implement the matching procedure. First, the size and location of the reference window have significant influence on the matching quality. Increasing window size leads to more uniqueness of the matching entity and also to more geometric distortions. Second, the size of the search window affects the duration of processing. Third, the location of the search window is important to provide good approximation for the matching process. Finally, the acceptance and rejection criteria, e.g. threshold values are to be determined carefully after a thorough analysis.

The size and location of the search window are related to the values of $x$ - and $y$-parallaxes. The value of $y$-parallax $\left(p_{y}\right)$, which differs from one point to another, is a function of the relative orientation between the two images. Such y-parallaxes can be reduced by bringing the images in epipolar geometry by using their exterior orientation parameters [7]. In epipolar images, lines connecting conjugate points are parallel to the x -axis of the image coordinate system and have the same $y$-coordinate. Accordingly, a point ( $\mathrm{x}^{\prime}, \mathrm{y}$ ) in the right image will be the conjugate of a point $(\mathrm{x}, \mathrm{y})$ in the left image if $\mathrm{x}^{\prime}=\mathrm{x}-\mathrm{p}_{\mathrm{x}}$ where $\mathrm{p}_{\mathrm{x}}$ is the x -parallax of the point. However, since $\mathrm{p}_{\mathrm{x}}$ is unknown, it can approximated by the photo base $b$ of the stereo pair. Thus the point ( $\mathrm{x}^{\prime}, \mathrm{y}$ ) where $\mathrm{x}^{\prime}$ $=\mathrm{x}-\mathrm{b}$ serves as the center of the search window. The size of the window in the x -direction is determined by a priori information on the elevation range of the object space. For images taken at height $H$ above a terrain with maximum elevation range $\Delta \mathrm{h}$, the maximum parallax range $\Delta \mathrm{p}$ is approximated by the formula $\Delta \mathrm{p}=\Delta \mathrm{h}(\mathrm{b} / \mathrm{H})$.

Before starting the correlation process, processing of digital data is usually required to correct for radiometric distortions. Preprocessing usually takes the form of image enhancement such as histogram equalization or linear stretching and filtering using a suitable filter, for example a mean or a median filter [9]. For correlation matching a radiometric adjustment is typically performed prior by equalizing the average and the standard deviation of gray levels of the two conjugate windows, thus accommodating for different radiometric properties of the two images.

The efficiency of correlation techniques can be considerably improved by the use of multiresolution matching utilizing image pyramid. An image pyramid is formed by successively convolving an image with a gaussian kernel, with each convolution producing a half-resolution copy of the previous image [6,9]. The series of images thus produced can be visualized as a stack of image layers forming a pyramid. By matching images in upper layers of the pyramid, the location of the match can be predicted in lower layers within a couple of pixels, which provides searching through the entire full-resolution image to find a matching feature.

## 4. The Proposed Procedure

In this section a semi-automatic approach is proposed to create DEMs from stereo digital imagery. In this procedure, fairly distinct feature points are specified by the operator in one image. By use of correlation matching, the positions of their conjugate points in the other image are found, to subpixel accuracy. The 3-D positions of the selected points are computed using least-square solution that is based on collinearity condition equations. The procedure is implemented on a PC using MATLAB software package. The proposed procedure can be described as follows:

1. Four fairly distinct points that exist in the four corners of the overlap area are identified and measured in the pixel coordinate system of each of the two images. The coordinates of the
four pairs are employed in a 2-D transformation to get roughly the conjugate position on the right image for any point specified on the left image.
2. The available control points are identified on the left image. Their coordinates are measured in the pixel coordinate system of the image. They would be used to introduce the datum in the adjustment process.
3. Numerous fairly distinct points on the left image are specified so that the entire image are covered and densified well. Their pixel coordinates are determined and recorded. These points would be the base on which the DEM is generated.
4. For each selected point in the left image, the location of its conjugate is found, to pixel accuracy, in the right image using correlation matching. The reference window is centered at the selected point in the left image whereas the search window is centered at the rough position of its conjugate in the right image.
5. Prototype software is developed to implement the matching process. The program defines the reference window with an appropriate size, enough to define the selected points. The location and the size of the search window are determined using preliminary knowledge about the photography and the terrain. The cross correlation coefficient is computed for every position of the matching window within the search window. The two images must have insignificant differences in scale and orientation; otherwise, they are to be adjusted before.
6. The program looks for the position with the highest correlation value and uses it as the optimal position of the conjugate point, provided that this value exceeds a specified threshold. The location of each conjugate point is found, to sub-pixel accuracy, by fitting a two-dimensional polynomial (with 6-parameters) to the nine pixels centered at the position with the highest correlation, and searching for the maximum. A function is appended to the cross correlation program to deal with this task.
7. For each of the two images, the transformation parameters necessary to convert from the pixel coordinate system, in which the measurements are captured, to the image coordinate systems are computed. This is carried out through the use of calibrated and measured coordinates of image fiducial marks in an affine transformation [5].
8. For each of the two images, convert the coordinates of selected points from the pixel coordinate system to the related image coordinate system.
9. The exterior orientation parameters for each of the two images are found utilizing a space resection procedure based on collinearity condition equations and sufficient ground control.
10. The 3-D coordinates of the collected points are computed using a space intersection process based on collinearity condition equations using the exterior orientation parameters computed formerly in the resection process.
11. The last two steps can be integrated in one simultaneous process (bundle adjustment). This solution provides reliable tools to identify deficient observations and to assess the quality of the whole process.
12. Having higher-resolution copy of the stereo pair, the locations of conjugate points, found in step no. 4, can serve as good approximations for their locations in the higher-resolution images. The coordinates of fiducial marks in both stereo pairs can be employed for the transformation of point coordinates between the corresponding images of the two pairs.

The DEM can be interpolated from the collected points with appropriate grid spacing and interpolation function by using one of available software packages of generating surfaces.

## 5. Experimentation

The test imagery consists of a stereo-pair of aerial photographs, covering an urban area. The scale of photography is nearly 1:2500. The photo pair is scanned with two different resolutions 600 dpi and 200 dpi, yielding nearly $42 \mu \mathrm{~m}$ - and $127 \mu \mathrm{~m}$-pixel-size stereo-pairs, respectively [4]. A set of
targets are affixed in the photographed area and their 3-D object coordinates are measured using precise terrestrial surveying to get their coordinates. The two images are shown in Figs. 1 and 2, respectively. For each stereo-pair, the coordinates of 4 fairly distinct points in the corners of the overlap area in both images as well as the coordinates of 4 control points and 90 fairly distinct points in the left image are measured using point selection module of MATLAB software. This module enables the user to navigate freely through the image and mark chosen points. The pixel coordinates of marked points are recorded directly by the module. Fig. 3 illustrates the locations of the used control points and the collected DEM points in the overlap area of the stereo pair.

The coordinates of the 4 corner pairs are employed in an affine transformation. The resulted transformation parameters are utilized to get coarsely the conjugate position on the right image for any point selected on the left image. The exact locations of conjugates of the selected points are found automatically, to sub-pixel accuracy, in the right image using the developed cross correlation program. The input data to the program are the pixel coordinates of selected points in the left image and of their coarsely-determined conjugates in the right image. The location of each coarselydetermined conjugate is used as the center of the search window in the right image. For the 200-dpi image pair, the size of the reference window is specified as 7 pixels by 7 pixels, which is enough to describe the selected points in the left image. The size of the search window is taken as 31 pixels by 31 pixels. A matching threshold of 0.6 is selected. The location of each conjugate point is found, to sub-pixel accuracy, by fitting a two-dimensional polynomial to the nine pixels centered at the position with the highest correlation, and searching for the maximum.

For each of the two Images, an affine transformation is employed to convert point coordinates from the pixel coordinate system to the image coordinate system, centered at the principal point. The
transformation parameters are computed using the calibrated coordinates of fiducial marks as well as their measured pixel coordinates through a least-squares procedure.

Prototype least-squares bundle adjustment software is developed in order to compute the exterior orientation parameters for each image and the adjusted object coordinates of collected points. Approximations for the exterior orientation parameters are found using the coordinates of the used control points in both image and object coordinate systems. Enhanced approximate values are obtained from a space resection for each of the two images utilizing ground control points. Approximations for the unknown ground coordinates of the collected points are generated from their coordinates on the left image using parameters of an affine transformation. The transformation is made utilizing ground coordinates of the control points and their left-image coordinates.

Two types of constraints are tried in the adjustment process to introduce absolute information: fixed constraints and inner constraints. Different sets of fixed constraints yield different estimates of the unknown parameters. On the other hand, inner-constraint solution has the minimum magnitude and variance of all possible solutions [1, 5].

The matching results of the 200 -dpi stereo pair are used to enhance the efficiency of matching the 600-dpi stereo pair. The coordinates of conjugate points in the 200-dpi right image, obtained by the matching program, are transformed to their equivalent values in the 600-dpi right image. These values serve as good approximations for the centers of the search window in the image. Since the image resolution of the second pair is higher than in the first pair, the size of the reference window is taken larger; 11 pixels by 11 pixels. However, the size of the search window is chosen to be only 21 pixels by 21 pixels due to the refined approximations of conjugate locations.

## 6. Results and Analysis

Regarding the used size of the reference and search windows, they were found suitable for detecting almost all conjugate points in the right image. Resulted correlation coefficients, associated with matched points, exceeded 0.8 . For the 200 -dpi stereo pair, only three conjugate are wrongly detected due to repetitive point pattern within the search window. However, the correct conjugate locations are reached by increasing the size of the reference window one more pixel in both directions. For the 600-dpi stereo pair, no matching ambiguities have occurred. This is clearly, in addition to the distinctness of selected points, due to adopting search window of limited size considering the related pixel size and size of reference window. This limited size is specified according to the nearly perfect position of the window center provided by the matching results of the 200 -dpi stereo pair. Table 1 presents the x , y image coordinates of selected points in the left image and their conjugates in the right image, found by the matching program.

Table 2 lists standard errors of estimated orientation elements of the left image for four solution setups. Corresponding values for the right image are depicted in Table 3. Table 4 gives resulted standard error of unit weight and standard errors of estimated ground-point coordinates in each of the adopted setups. Listed below are the abbreviations used in those tables:
$\sigma_{\text {om }}, \sigma_{\text {phi }}, \sigma_{\text {kap }} \quad$ resulted standard errors of estimated orientation angles $(\omega, \varphi, \kappa)$;
$\sigma_{\mathrm{XL}}, \sigma_{\mathrm{YL}}, \sigma_{\mathrm{ZL}} \quad$ resulted standard errors of estimated coordinates of camera perspective center;
$\sigma_{\mathrm{X}}, \sigma_{\mathrm{Y}}, \sigma_{\mathrm{Z}} \quad$ resulted standard errors of estimated coordinates of ground point; and
Ave, Max average and maximum values.
According to the precision figures listed in the Tables 2,3 and 4, it is clear that the precision gets better at using 600-dpi stereo pair, compared with the 200 -dpi stereo pair. Also, the inner-constraint solution has led to better results for both resolutions, compared with the fixed-constraint solution. The resulted standard error of unit weight $\left(\sigma_{0}\right)$ in each of the four setups indicates the precision of
measured coordinates of matched image points that reached a fraction of a pixel; about one half of a pixel for the 600 -dpi stereo pair and nearly one fifth of a pixel for the 200 -dpi stereo pair. This denotes the superior precision obtainable by the adopted matching procedure.

Finally, standard errors of computed 3-D ground coordinates of DEM points indicate the good precision resulted utilizing the selected DEM points, although they normally represent natural features. This is due to the fair distinctness of those points that has led to minimal matching ambiguities and high-quality matching precision

Table 1: x,y Image Coordinates of Selected Points in the Left Image and Their
Conjugates in the Right image, Found by Correlation Matching

| Pt. | Left Image |  | Right Image |  | Pt. | Left Image |  | Right Image |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | x | y | x | y |  | x | y | x | y |
| 1 | -42.111 | 101.745 | -109.740 | 97.317 | 46 | 106.164 | 3.081 | 37.899 | -0.533 |
| 2 | -23.058 | 103.959 | -90.703 | 99.451 | 47 | 89.070 | -15.514 | 20.798 | -19.105 |
| 3 | -3.394 | 100.458 | -70.986 | 95.911 | 48 | 64.684 | -17.644 | -3.869 | -21.408 |
| 4 | 10.084 | 104.343 | -57.377 | 99.685 | 49 | 48.052 | -17.835 | -20.512 | -21.673 |
| 5 | 32.411 | 99.690 | -35.232 | 94.988 | 50 | 22.798 | -15.076 | -46.129 | -18.984 |
| 6 | 40.454 | 112.860 | -26.893 | 107.800 | 51 | 6.288 | -16.220 | -62.807 | -20.214 |
| 7 | 62.485 | 98.816 | -5.430 | 94.057 | 52 | -15.142 | -10.173 | -84.707 | -14.124 |
| 8 | 82.664 | 97.154 | 14.602 | 92.366 | 53 | -34.315 | -10.482 | -104.027 | -14.522 |
| 9 | 111.185 | 86.576 | 42.657 | 81.961 | 54 | -31.739 | -31.308 | -101.753 | -35.599 |
| 10 | 93.036 | 85.190 | 24.712 | 80.657 | 55 | -9.185 | -41.927 | -78.956 | -46.311 |
| 11 | 80.208 | 83.968 | 11.974 | 79.482 | 56 | -6.174 | -20.806 | -75.734 | -24.914 |
| 12 | 69.104 | 82.215 | 0.950 | 77.804 | 57 | 41.901 | -30.822 | -26.817 | -34.791 |
| 13 | 51.611 | 79.986 | -16.325 | 75.661 | 58 | 7.090 | -36.403 | -62.224 | -40.609 |
| 14 | 35.918 | 76.845 | -31.956 | 72.619 | 59 | 22.922 | -45.220 | -46.336 | -49.480 |
| 15 | 16.398 | 75.478 | -51.464 | 71.274 | 60 | 68.146 | -39.106 | -0.531 | -43.026 |
| 16 | -5.407 | 83.175 | -73.331 | 78.990 | 61 | 63.505 | -55.335 | -5.276 | -59.527 |
| 17 | -23.074 | 80.011 | -91.077 | 75.880 | 62 | 46.222 | -59.078 | -22.707 | -63.432 |
| 18 | -41.798 | 75.117 | -110.030 | 71.096 | 63 | 46.401 | -47.275 | -22.562 | -51.433 |
| 19 | -41.837 | 54.223 | -110.568 | 50.335 | 64 | 94.051 | -38.124 | 25.676 | -41.855 |
| 20 | -20.105 | 59.346 | -88.527 | 55.400 | 65 | 97.022 | -55.524 | 28.601 | -59.494 |
| 21 | 17.236 | 57.796 | -51.075 | 53.808 | 66 | 106.752 | -36.903 | 38.457 | -40.604 |
| 22 | -3.473 | 55.081 | -71.959 | 51.145 | 67 | 92.878 | -74.293 | 24.420 | -78.587 |

Table 1 (continued)

| Pt. | Left Image |  | Right Image |  | Pt. | Left Image |  | Right Image |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | x | y | x | y |  | x | y | x | y |
| 23 | 43.328 | 58.135 | -24.931 | 54.112 | 68 | 73.557 | -79.551 | 4.822 | -84.065 |
| 24 | 61.607 | 57.432 | -6.641 | 53.397 | 69 | -31.880 | -63.990 | -102.545 | -68.936 |
| 25 | 78.118 | 64.590 | 9.995 | 60.410 | 70 | -10.919 | -61.022 | -81.009 | -65.764 |
| 26 | 96.752 | 57.793 | 28.394 | 53.723 | 71 | -34.232 | -50.083 | -104.698 | -54.736 |
| 27 | 111.072 | 51.775 | 42.624 | 47.792 | 72 | 35.920 | -63.292 | -33.253 | -67.790 |
| 28 | 111.264 | 37.466 | 42.769 | 33.656 | 73 | 10.381 | -67.892 | -59.320 | -72.646 |
| 29 | 86.751 | 35.273 | 18.467 | 31.474 | 74 | 7.913 | -51.383 | -61.660 | -55.826 |
| 30 | 64.315 | 34.778 | -4.001 | 30.990 | 75 | -31.497 | -92.803 | -102.586 | -98.544 |
| 31 | 44.325 | 36.344 | -23.948 | 32.531 | 76 | -10.259 | -84.505 | -80.664 | -89.806 |
| 32 | -3.774 | 30.859 | -72.386 | 27.054 | 77 | -26.863 | -78.224 | -97.682 | -83.474 |
| 33 | 19.344 | 34.454 | -49.013 | 30.679 | 78 | -16.409 | -97.555 | -87.190 | -103.283 |
| 34 | -21.770 | 38.937 | -90.382 | 35.097 | 79 | -2.332 | -101.225 | -72.747 | -106.976 |
| 35 | -42.111 | 32.667 | -110.988 | 28.863 | 80 | 10.580 | -80.649 | -59.229 | -85.687 |
| 36 | -40.685 | 14.009 | -110.148 | 10.155 | 81 | 26.798 | -88.198 | -42.716 | -93.299 |
| 37 | -19.242 | 10.882 | -88.285 | 7.029 | 82 | 50.975 | -81.510 | -18.120 | -86.244 |
| 38 | 2.991 | 10.377 | -65.911 | 6.550 | 83 | 38.417 | -108.244 | -31.193 | -113.844 |
| 39 | 21.132 | 7.770 | -47.319 | 3.941 | 84 | 67.251 | -105.052 | -1.918 | -110.250 |
| 40 | 33.573 | 7.343 | -35.058 | 3.567 | 85 | 47.755 | -92.287 | -21.578 | -97.394 |
| 41 | 63.971 | 5.143 | -4.451 | 1.444 | 86 | 13.678 | -104.027 | -56.412 | -109.715 |
| 42 | 83.772 | 4.053 | 15.463 | 0.395 | 87 | 96.976 | -101.470 | 28.421 | -106.267 |
| 43 | 57.429 | 19.002 | -10.970 | 15.269 | 88 | 97.783 | -90.938 | 29.314 | -95.524 |
| 44 | 99.764 | 20.494 | 31.424 | 16.821 | 89 | 27.208 | -28.800 | -41.789 | -32.813 |
| 45 | 73.857 | 18.814 | 5.536 | 15.120 | 90 | -30.717 | 23.709 | -99.706 | 19.868 |

Table 2: Resulted Standard Errors of Estimated Orientation Elements of
the Left Image in Different Solution Setups

| Statistic | Fixed-Constraint <br> Solution <br> (600-dpi Pair) | Inner-Constraint <br> Solution <br> (600-dpi Pair) | Fixed-Constraint <br> Solution <br> (200-dpi Pair) | Inner-Constraint <br> Solution <br> (200-dpi Pair) |
| :---: | :---: | :---: | :---: | :---: |
| $\sigma_{\text {om }}$ | 1.7748 | 0.5886 | 2.4341 | 0.7800 |
| $\sigma_{\text {phi }}$ | 1.2948 | 0.5649 | 2.4341 | 0.7486 |
| $\sigma_{\text {kap }}$ | 0.3918 | 0.1128 | 0.5379 | 0.1495 |
| $\sigma_{\mathrm{XL}}$ | 0.1570 | 0.0754 | 0.2157 | 0.0998 |
| $\sigma_{\mathrm{YL}}$ | 0.2157 | 0.0715 | 0.2958 | 0.0948 |
| $\sigma_{\mathrm{ZL}}$ | 0.0605 | 0.0223 | 0.0829 | 0.0296 |

Units: $\sigma_{\mathrm{om}}, \sigma_{\mathrm{phi}}, \sigma_{\mathrm{kap}}$ are in minutes; and $\sigma_{\mathrm{XL}}, \sigma_{\mathrm{YL}}, \sigma_{\mathrm{ZL}}$ are in meters.

Table 3: Resulted Standard Errors of Estimated Orientation Elements of the Right Image in Different Solution Setups

| Statistic | Fixed-Constraint <br> Solution <br> $(600-\mathrm{dpi}$ Pair) | Inner-Constraint <br> Solution <br> (600-dpi Pair) | Fixed-Constraint <br> Solution <br> (200-dpi Pair) | Inner-Constraint <br> Solution <br> (200-dpi Pair) |
| :---: | :---: | :---: | :---: | :---: |
| $\sigma_{\text {om }}$ | 1.7171 | 0.5779 | 2.3550 | 0.7686 |
| $\sigma_{\text {phi }}$ | 1.3083 | 0.5810 | 1.7974 | 0.7700 |
| $\sigma_{\text {kap }}$ | 0.3902 | 0.1189 | 0.5357 | 0.1576 |
| $\sigma_{\mathrm{XL}}$ | 0.1613 | 0.0782 | 0.2246 | 0.1036 |
| $\sigma_{\mathrm{YL}}$ | 0.2054 | 0.0701 | 0.2816 | 0.0929 |
| $\sigma_{\mathrm{ZL}}$ | 0.07217 | 0.0227 | 0.0990 | 0.0301 |

Units: $\sigma_{\mathrm{om}}, \sigma_{\mathrm{phi}}, \sigma_{\mathrm{kap}}$ are in minutes; and $\sigma_{\mathrm{XL}}, \sigma_{\mathrm{YL}}, \sigma_{\mathrm{ZL}}$ are in meters.

Table 4: Resulted Standard Error of Unit Weight ( $\sigma_{0}$ ) and Standard Errors of Estimated Ground-Point Coordinates in Different Solution Setups

| Statistic | Fixed-Constraint <br> Solution <br> $(600-$ dpi Pair) | Inner-Constraint <br> Solution <br> $(600-d p i$ Pair) | Fixed-Constraint <br> Solution <br> $(200-\mathrm{dpi}$ Pair) | Inner-Constraint <br> Solution <br> (200-dpi Pair) |
| :---: | :---: | :---: | :---: | :---: |
| $\sigma_{0}$ | 19.4000 | 17.3000 | 26.6000 | 23.0000 |
| Ave $\sigma_{X}$ | 0.0826 | 0.0618 | 0.1134 | 0.0820 |
| Max $\sigma_{X}$ | 0.1484 | 0.1121 | 0.2035 | 0.1488 |
| Ave $\sigma_{Y}$ | 0.0687 | 0.0493 | 0.0944 | 0.0653 |
| Max $\sigma_{Y}$ | 0.1298 | 0.0970 | 0.1783 | 0.1288 |
| Ave $\sigma_{Z}$ | 0.1947 | 0.1384 | 0.2671 | 0.1835 |
| Max $\sigma_{Z}$ | 0.2259 | 0.1412 | 0.3097 | 0.1881 |
| Unis $\sigma_{i}$ |  |  |  |  |

Units: $\sigma_{0}$ is in $\mu \mathrm{m}$; and Ave $\sigma_{\mathrm{X}}, \operatorname{Max} \sigma_{\mathrm{X}}$, Ave $\sigma_{\mathrm{Y}}, \operatorname{Max} \sigma_{\mathrm{Y}}$, Ave $\sigma_{\mathrm{Z}}, \operatorname{Max} \sigma_{\mathrm{Z}}$ are in meters.

## 7. Conclusions

In this research, a semi-automatic approach is presented to generate DEMs from stereo digital imagery. In this procedure, the operator points to points of interest in one image and their conjugate points are found, to sub-pixel accuracy, by use of matching. This would enable having suitable matching entities, leading to good matching results. The procedure is implemented on a PC using MATLAB software package. The test imagery consists of a stereo-pair of aerial photographs, covering an urban area. The scale of photography is nearly 1:2500. The photo pair is scanned with two different resolutions: 600 dpi and 200 dpi . A set of targets is affixed in the photographed area and measured using precise terrestrial surveying. A total of 90 feature points in the overlapping area are selected and matched using correlation technique through prototype software developed in the MATLAB environment. The 3-D positions of the selected points are computed using bundle adjustment with fixed as well as inner constraints.

According to the results achieved in this research, a number of conclusions can be drawn as follows:

- Due to the power of modern PC platforms, automating DEM generation and other digital photogrammetric procedures can be implemented on PCs.
- The use of multi-resolution correlation matching employing multi-resolution imagery leads to finer approximations, smaller search-window sizes and thus to lesser matching cost and ambiguities.
- Utilizing smaller image pixel sizes enhance the precision of the matching results and the overall adjustment results as well. However, more powerful hardware and software will be required.
- An optimal value of image pixel size is to be found in order to reach the desired DEM accuracy with minimum cost.
- The use of inner-constraint solution is recommended for obtaining improved precision figures.
- To fully automate the entire DEM generation procedure, the presented approach needs one further step; the left-image points are to be derived automatically using feature extraction techniques.


## References

(1) B. Schaffrin, Advanced Adjustment Computatios, Class Notes, Geodetic Science Dept., The Ohio State University, Columbus, OH. (1994)
(2) C. Heipke, ISPRS Journal of Photogrammetry and Remote Sensing, Vol. 52, No.1, 1 (1997).
(3) C. Heipke, Photogrammetric Engineering and Remote Sensing, Vol. 61, No.1, 49 (1995).
(4) DVP Geomatic Systems, DVP Software., DVP Geomatic Systems Inc. (1997).
(5) E.M. Mikail, J.S. Bethel and J.C. McGlone, Introduction to Modern Photogrammetry, John Wiley \& Sons, Inc., New York (2001).
(6) P.R. Wolf and B.A.Dewitt, Elements of Photogrammetry, McGraw Hill, Inc., New York (2000).
(7) T. Schenk, Digital Photogrammetry, Laurelville, OH: TerraScience (1999).
(8) T. Schenk, J.C. Li and C. Toth, Photogrammetric Engineering and Remote Sensing, Vol. 57, No.8, 1057 (1991)
(9) W. K. Pratt, Digital Image Processing, John Wiley \& Sons, Inc., New York (1991).
(10) Y. Lue, International Archives of Photogrammetry and Remote Sensing, Vienna, Austria, Vol. XXXI, 476 (1996).


Figure 1: The Left Image of the Test Stereo Pair


Figure 2: The Right Image of the Test Stereo Pair


Figure 3: The Configuration of Control and DEM Points in the Overlap Area of the Stereo Pair

